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JOLY Amaury

**Encadrants** : GODARD Emmanuel, TRAVERS Corentin

*Aix-Marseille Université, Scille*

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# 1 Introduction

## 1.1 Model

### 1.1.1 Model Properties

The model is defined as Message-passing Aysnchronous.

There is  $n$  process. Each process is associated to a unique unforgeable id  $i$ .

Each process know the identity of all the process in the system

Each process have a reliable communication channel with all the others process such as :

- $\text{send}(m)$  is the send primitive
- $\text{recv}(m)$  is the reception primitive

A message send is eventually received

The system is Crash-Prone. There is at most  $f$  process who can crash such as  $f < n$ .

### 1.1.2 AtomicBroadcast Properties

**Property 1** *AB\_broadcast Validity* if a message is sent by a correct process, the message is eventually received by all the correct process.

**Property 2** *AB\_receive Validity* if a message is received by a correct process, the message is eventually received by all the correct process.

**Property 3** *AB\_receive safety No creation* if a message is received by a correct process, the message was emitted by a correct porcess.

**Property 4** *AB\_receive safety No duplication* each message is received at most 1 time by each process.

**Property 5** *AB\_receive safety Ordering*  $\forall m_1, m_2$  two messages,  $\forall p_i, p_j$  two process.  
if  $AB\_recv(m_1)$  and  $AB\_recv(m_2)$  for  $p_i, p_j$   
and  $AB\_recv(m_1)$  is before  $AB\_recv(m_2)$  for  $p_i$   
so  $AB\_recv(m_1)$  is before  $AB\_recv(m_2)$  for  $p_j$

### 1.1.3 DenyList Properties

**Property 6** *APPEND Validity* a  $APPEND(x)$  is valid iff the process  $p$  who sent the operation is such as  $p \in \Pi_M$ . And iff  $x \in S$  where  $S$  is a set of valid values.

**Property 7** *PROVE Validity* a  $PROVE(x)$  is valid iff the process  $p$  who sent the operation is such as  $p \in \Pi_V$ . And iff  $\exists APPEND(x)$  who appears before  $PROVE(x)$  in Seq.

**Property 8** *PROGRESS* if an  $APPEND(x)$  is invoked, so there is a point in the linearization of the operations such as all  $PROVE(x)$  are valids.

**Property 9** *READ Validity*  $READ()$  return a list of tuples who is a random permutation of all valids  $PROVE()$  associated to the identity of the emiter process.

## 1.2 Algorithms

We define  $k$  as the id of the round  
the  $getMax(..)$  function able to return the highest round played in the system.

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**Algorithm 1:** AB\_Broadcast

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**Input:** le message  $m$

```
1 while true do
2   proves = READ()
3   k = getMax(dump) + 1
4   APPEND(k || m)
5   if PROVE(k) then
6     APPEND(k)
7     return
8   end
9 end
```

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We define  $k\_max$  as an intager

$getMax(..)$  function able to return the highest round played in the system.

$proves_r \subseteq proves$  s.a.  $\forall PROVE(x) \in proves_r$ ,  $x$  is in the form  $r||m$  with  $m$  who cannot be empty  
 $proves_r^i$  is the  $PROVE(r||m)$  operation submitted by the process  $i$  if exist

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**Algorithm 2:** AB\_Listen

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```
1 while true do
2   proves = READ()
3   k_max = getMax(proves)
4   for r=k+1 to k_max do
5     APPEND(r)
6     proves_r = READ();
7     for i = 1 to |proves_r| do
8       AB_Recv(proves_r^i)
9     end
10  end
11 end
```

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